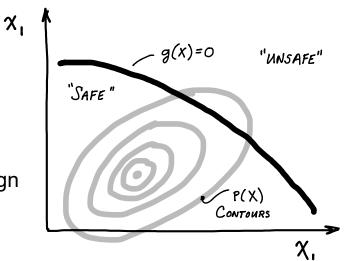


CIEM42X0 Probabilistic Design

<u>3 main topics</u>: extreme value analysis, component reliability, system reliability

Objective: learn how the methods can be used to gain insight and improve your design





Patricia Mares Nasarre Extreme value analysis



Robert Lanzafame Component Reliability

Oswaldo Morales Nápoles System Reliability



CIEM42X0 Probabilistic Design

<u>3 main topics</u>: extreme value analysis, component reliability, system reliability

Objective: learn how the methods can be used to gain insight and improve your design

Course setup:

- Tuesday lecture, Friday workshop
- Various assignments (homework or in-class workshops on Friday)
- 3 workshops submitted for feedback/grade (weeks 2, 5, 8) \rightarrow more info coming; weeks might be updated!

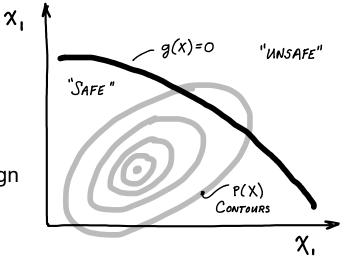
Unit Website(s): textbook links, calendar, announcements, logistics, etc

Assessment: incorporated in projects and exams for each unit \rightarrow use code from assignments!

Contact Patricia Mares Nasarre for questions.

→ bookmark the website!
→ The comp-mod site too!
<u>tudelft-citg.github.io/HOS-prob-design-25/</u>
<u>tudelft-citg.github.io/HOS-comp-mod-25/</u>





Demonstration (not on slides)

- Website
- Online Textbook
- This week
 - Read Chapter 1
 - Review MUDE
 - Set up your environment



Programming

This will be homework \rightarrow Python setup \odot

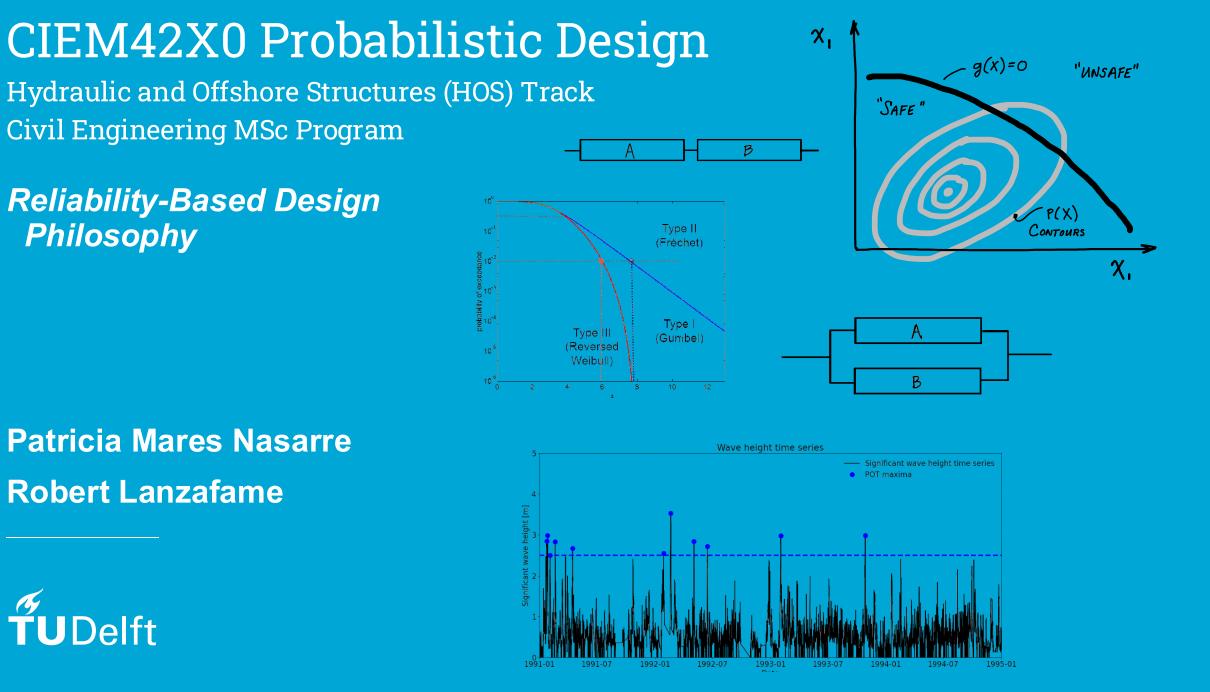
- "You need to set up a new environment by Friday week 2 (for week 1, MUDE env should work)
 - pyExtremes
 - OpenTURNs
 - GitHub
- Env instructions provided in the webpage: <u>https://tudelft-citg.github.io/HOS-prob-design-25/</u>



Summary

- Review MUDE weeks 1.7 & 1.8
- Set up your new environment
- Let Patricia know if you have questions!





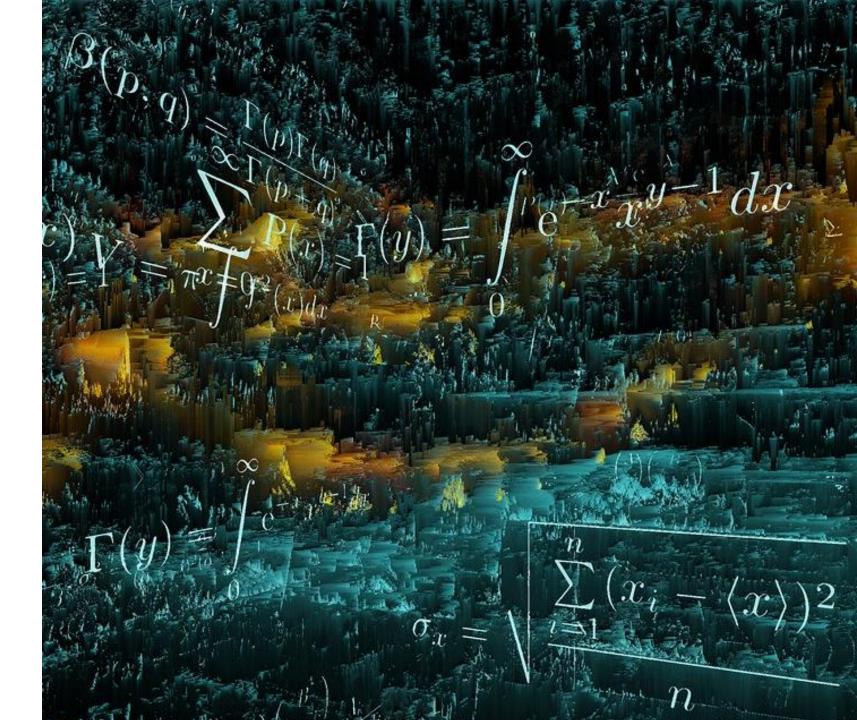
Outline

1. Refresher: univariate distributions

2. Risk analysis

3. Reliability analysis





1. Univariate (continuous) distributions – What's that?



- Univariate \rightarrow 1 variable
- Continuous → Continuous variables (not discrete)
- Univariate (continuous) distributions:
 - Mathematical model which relates the values of a random variable and their probability

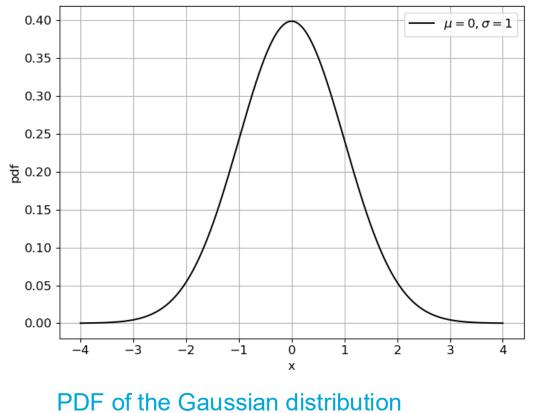




1. Univariate (continuous) distributions – PDF

- Continuous random variables
- Mathematical model which relates the values of a random variable and their probability
- Probability **density** function (PDF) $f_X(x)$
 - $egin{aligned} &f_X(x)dx = P(x < X \leq x + dx) \ &f_X(x) \geq 0 \ &\int_{-\infty}^{+\infty} f_X(x)dx = 1 \end{aligned}$





$$f(x)=rac{1}{\sigma\sqrt{2\pi}}e^{-rac{1}{2}(rac{x-\mu}{\sigma})^2}$$

1. Univariate (continuous) distributions - From PDF to CDF

• Probability density function (PDF) $f_X(x)$

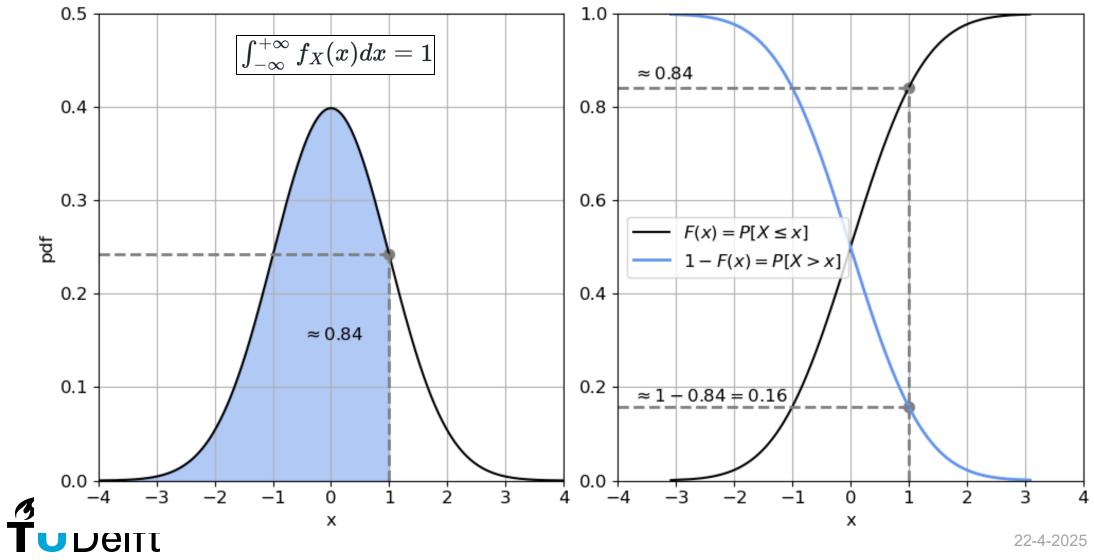
0.5 1.0 $-\mu = 0, \sigma = 1$ $\mu = 0, \sigma = 1$ 0.4 0.8 0.3 0.6 pdf 0.2 (x) 0.4 0.1 0.2 0.0 |- -4 0.0 +- -4 -2 _1 -3 2 -3 -2 2 3 0 1 3 -1 0 х х **U**Delft 22-4-2025 11

 $PDF \rightarrow how? \rightarrow CDF$

Cumulative distribution function (CDF) $F(x) = \int_{-\infty}^{x} f(x) dx$ $F(x) = \frac{1}{2} \left(1 + \operatorname{erf} \left(\frac{x - \mu}{\sigma \sqrt{2}} \right) \right)$

CDF of the Gaussian distribution

1. Univariate (continuous) distributions – exceedance

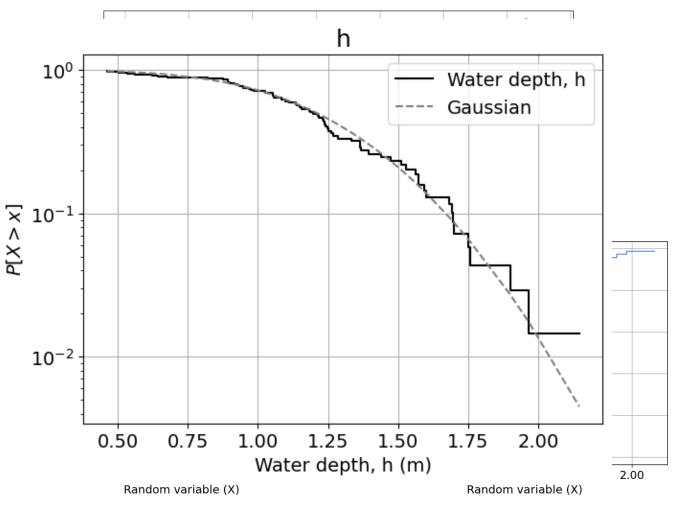


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1. Univariate distributions – how do we fit it to data?

Given a parametric distribution function (e.g.: Gaussian distribution):

- 1. Build ECDF from the data
- 2. Fit the distribution to the ECDF using method of moments or MLE
- 3. Goodness of fit: graphical methods or hypothesis test
- 4. Is it good enough for your purposes? Then, use it!





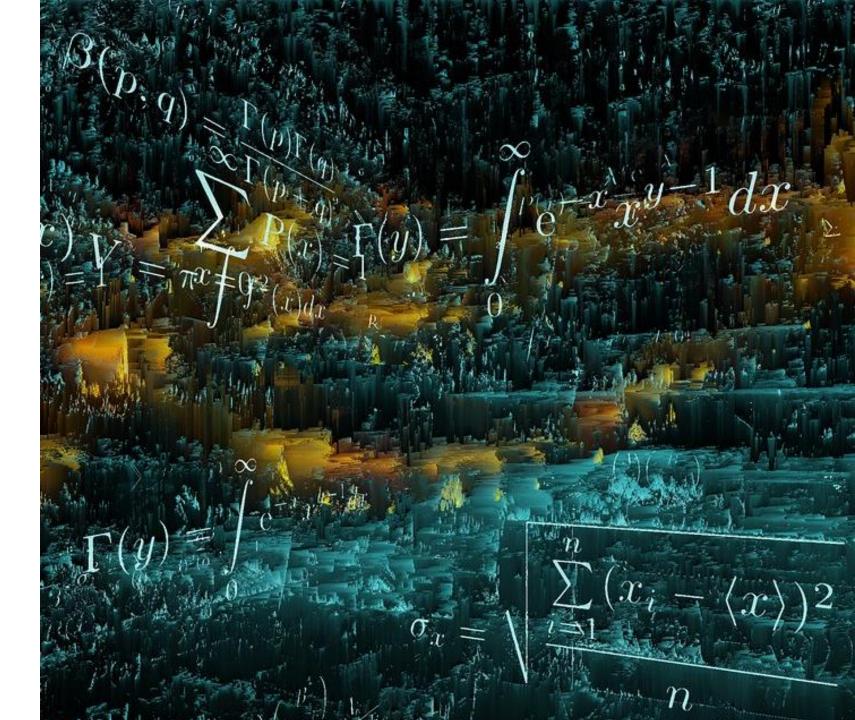
Outline

1. Refresher: univariate distributions

2. Risk analysis

3. Reliability analysis





2. Risk Analysis – what is risk?

"a situation involving exposure to danger" \rightarrow focused on consequences

"the possibility that something unpleasant or unwelcome will happen" \rightarrow focused on the probability of happening

 $E(d_i) = p_i \cdot d_i$

Which definition do we typically use?

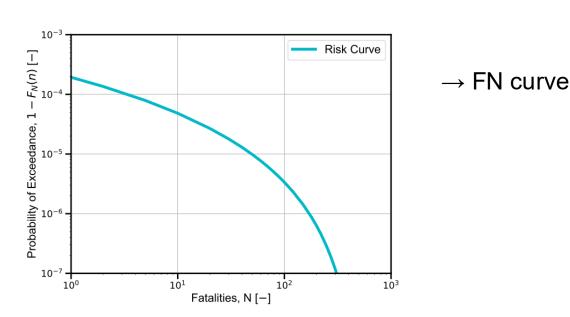
Risk is the probability of an undesired event multiplied by the consequences.

Expected damage for a given set of scenarios i=1,..., n

$$E(d) = \sum_{S_{i=1}}^n p_i \cdot d_i$$

But what are the contributions to that risk? Is there a scenario with very high consequences? Or very likely to occur? \rightarrow Risk curve

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€/year

Expected damage,

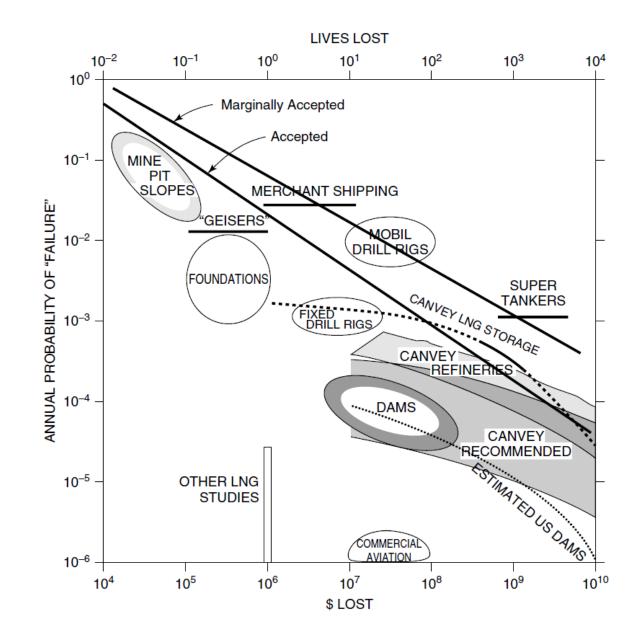
typically expressed in

2. Risk Analysis – why?

Why do we use the concept of risk?

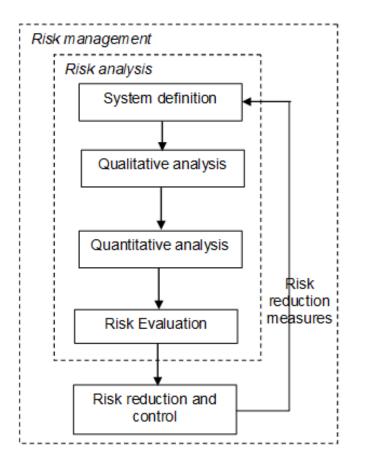
- Decide on acceptability
- Safety levels in the design process
- Need for measures in existing systems

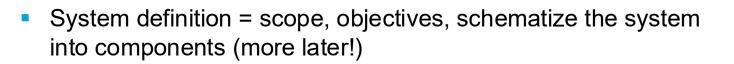
Quantitative measure to transfer from decisions to technical field.





2. Risk Analysis – Steps





- Qualitative analysis = undesired events and consequences. How the system can fail
- Quantitative analysis = quantification of risk; component and system reliability and consequences
- Risk evaluation = decision, is it acceptable?
- First four steps repeated several times to reach an optimal design



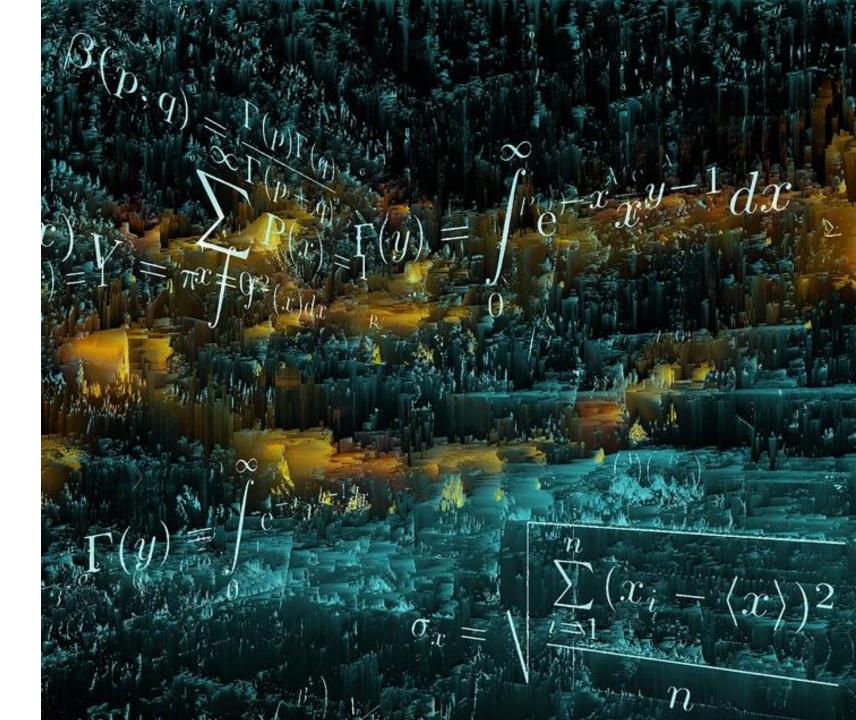
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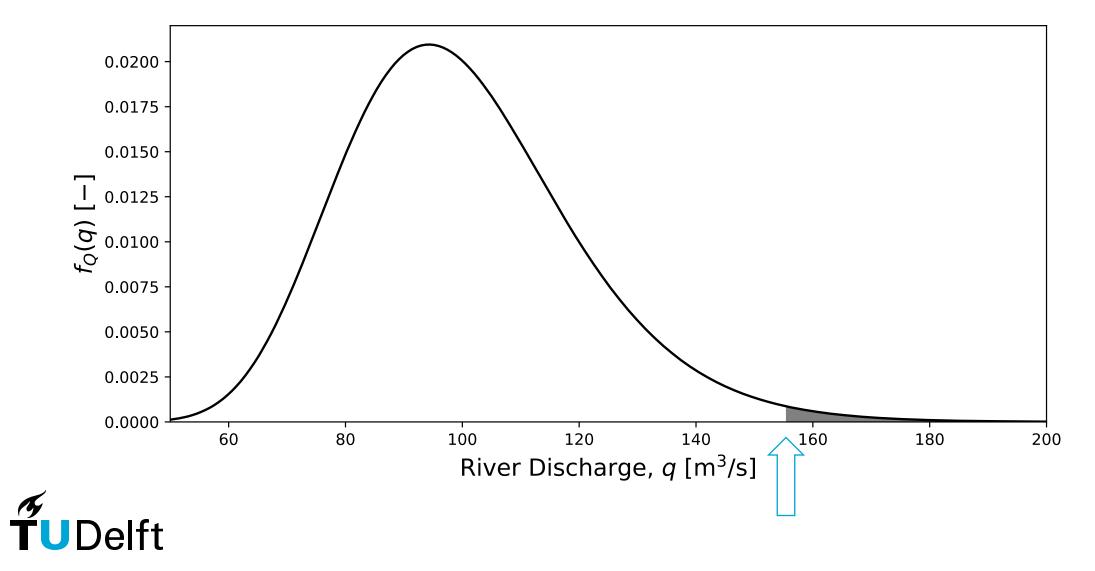
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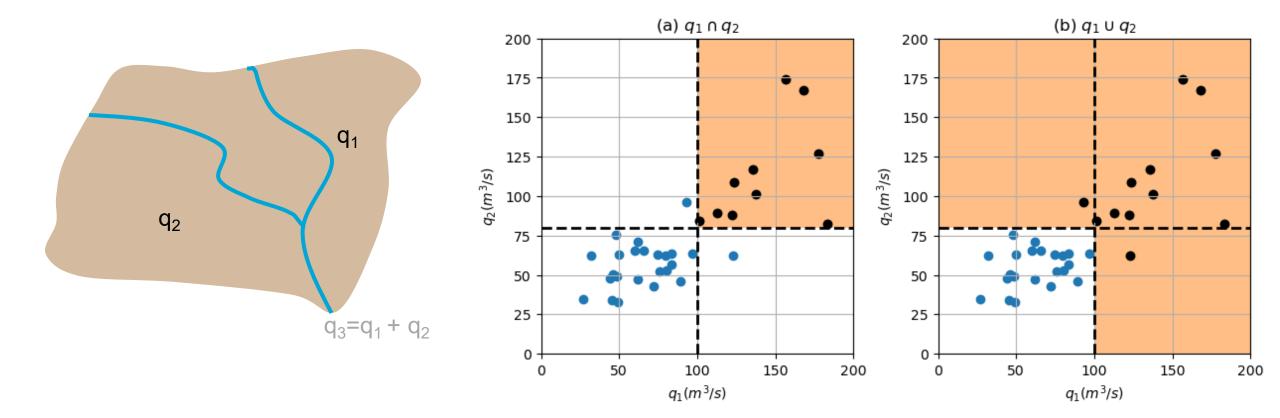




3. Reliability Analysis – how do we define failure?

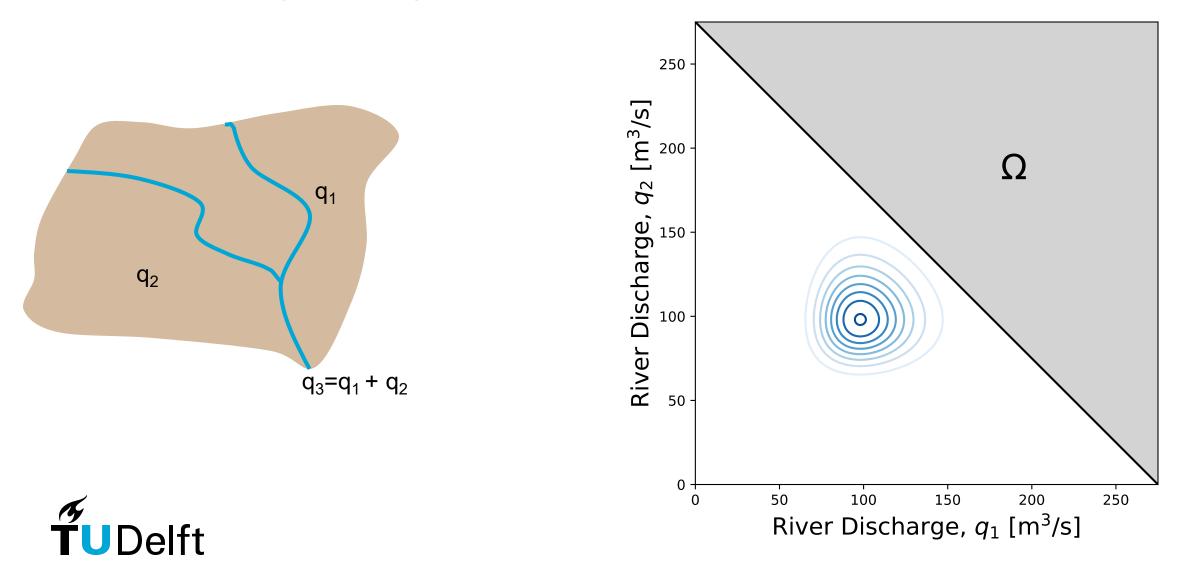


3. Reliability Analysis – how do we define failure?

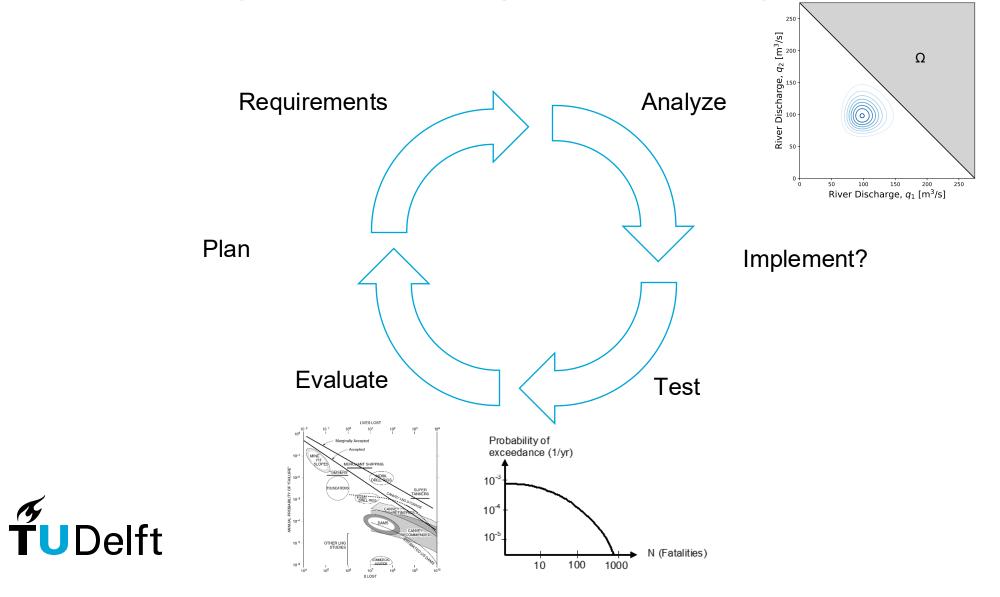




3. Reliability Analysis – how do we define failure?



3. Reliability-Based Design Philosophy



How we will approach reliability-based design

- Risk Analysis: evaluation, assessment, context (MUDE)
- Continuous Distributions, Extreme Value Analysis (MUDE, Week 2)
- Dependence touched lightly (covered in cross-over!!! CEGM2005 <u>tudelft-citg.github.io/MORE</u>)
- Component Reliability: a function of random variables $p_f = \int_{\Omega} f_X(x) dx$
- System Reliability: solving complex systems



Summary of Reliability-Based Design Philosophy

- Reliability methods for analysing and evaluating structures/system
- Risk analysis provides a framework for evaluation
- We will apply this to your design case in our unit!

